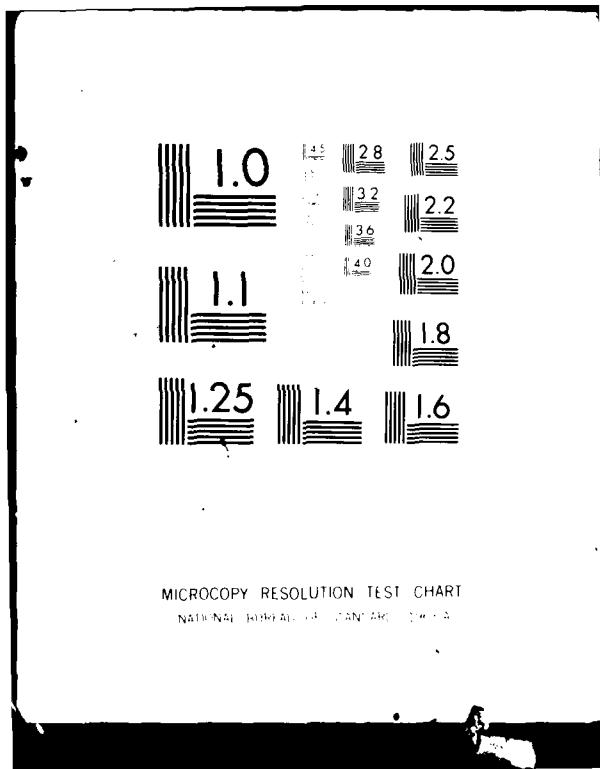


AD-A098 739 NOTRE DAME UNIV IN DEPT OF ELECTRICAL ENGINEERING F/G 12/1
A COMPARISON OF FREQUENCY-DOMAIN APPROACH AND TIME-DOMAIN APPROX--ETC(U)
MAY 80 C LIN N00014-78-C-0444
UNCLASSIFIED EE-802 NL

101
A
REF ID: A62642

END
DATE FILMED
8-88
DTIC



MICROCOPY RESOLUTION TEST CHART

NATIONAL INSTRUMENTS CORPORATION

PHOTOGRAPH THIS SHEET

AD A 098 739

DTIC ACCESSION NUMBER

II

LEVEL

I

INVENTORY

A COMPARISON OF FREQUENCY-DOMAIN APPROACH
AND TIME-DOMAIN APPROACH: A CASE STUDY OF
FAULT ANALYSIS OF ANALOG CIRCUITS

DOCUMENT IDENTIFICATION

N 00014-75-C-0498

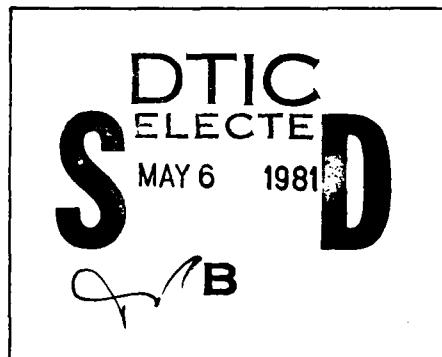
DISTRIBUTION STATEMENT A

Approved for public release;
Distribution Unlimited

DISTRIBUTION STATEMENT

ACCESSION FOR	
NTIS	GRA&I
DTIC	TAB
UNANNOUNCED	
JUSTIFICATION	
DR. KP 5/6/81	
BY	
DISTRIBUTION /	
AVAILABILITY CODES	
DIST	AVAIL AND/OR SPECIAL
A	

DISTRIBUTION STAMP



DATE ACCESSIONED

81 4 27 155

DATE RECEIVED IN DTIC

PHOTOGRAPH THIS SHEET AND RETURN TO DTIC-DDA-2

AD A098739

A COMPARISON OF FREQUENCY-DOMAIN APPROACH
AND TIME-DOMAIN APPROACH: A Case Study of
Fault Analysis of Analog Circuits

by

Chen-Shang Lin

Technical Report No. EE-802

May 23, 1980

This report was supported in part by the Office of Naval Research under
Grant N0014-78-C-0444. *N00014-75-C-0498*

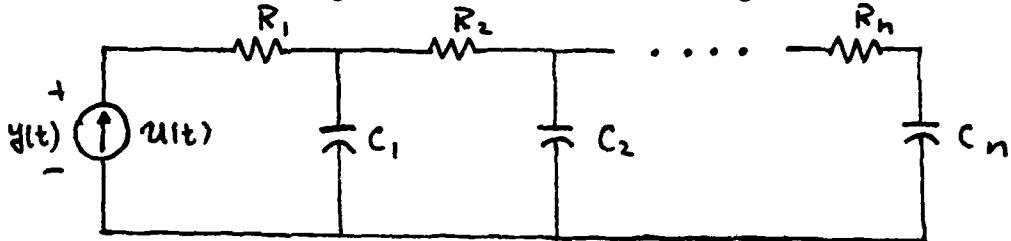
81 4 27 155

I. Introduction

There have been considerable efforts expended in analog fault analysis. Most of them [1], [2], [3] employ frequency-domain approach, i.e., diagnosing faulty components from measured transfer function, while few [5] use time-domain approach to isolate faults by means of Markov parameters. Theoretically, both approaches are still under development and all seem feasible. It is the purpose of this report to compare these two approaches numerically by simulation on RC ladders. In this example, it is shown that the time-domain approach is far better than the frequency-domain approach.

II. Simulation and Results

Consider an n -stage RC ladder as shown in Figure 1.



The impedance $Z(s)$ of this RC-ladder has the form

$$Z(s) = \frac{a_0 s^n + a_1 s^{n-1} + \dots + a_n}{s^n + b_1 s^{n-1} + \dots + b_n}$$

Since there are only $(2n+1)$ coefficients to be determined, we need only to measure the impedance $Z(s_i)$ at $(2n+1)$ different sampling frequencies, s_i , $i = 1, 2, \dots, (2n+1)$.

Once $Z(s)$ is obtained, it can be expressed as

$$Z(s) = R_1 + \frac{1}{C_1 s + \frac{1}{\vdots}} + \frac{1}{R_1 + \frac{1}{C_2 s + \frac{1}{\vdots}}} + \frac{1}{R_n + \frac{1}{C_n s}}$$

and values of components can be calculated as

$$\begin{aligned} R_1 &= \lim_{s \rightarrow \infty} \frac{N_1(s)}{D_1(s)} \\ C_1 &= \lim_{s \rightarrow \infty} \frac{D_2(s)}{N_1(s)} \\ R_i &= \lim_{s \rightarrow \infty} \frac{N_i(s)}{D_i(s)} \\ C_i &= \lim_{s \rightarrow \infty} \frac{D_{i+1}(s)}{N_i(s)} \quad i = 2, 3, \dots, n \end{aligned} \tag{1}$$

where

N_1 = numerator polynomial of Z

D_1 = denominator polynomial of Z

$N_i = N_{i-1}(s) - C_{i-1} \cdot D_i(s)$

$D_i = D_{i-1}(s) - R_{i-1} \cdot N_{i-1}(s)$

On the other hand, the ladder has a state equation expression

$$\dot{\underline{x}} = \underline{Ax} + \underline{Bu}$$

$$y = \underline{Cx} + \underline{Du}$$

where \underline{x} are the capacitor voltages, u the terminal current, y the terminal voltage and

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} -\frac{1}{R_2C_1} & \frac{1}{R_2C_1} & 0 & \frac{1}{C_1} \\ \frac{1}{R_2C_2} & \left(\frac{-1}{R_2C_2} - \frac{1}{R_3C_2}\right) & \frac{1}{R_3C_2} & 0 \\ \vdots & \ddots & \ddots & \vdots \\ 0 & \ddots & \ddots & \frac{1}{R_nC_{n-1}} \\ \hline 1 & 0 & \ddots & \frac{1}{R_nC_n} \\ \hline & & & \frac{-1}{R_nC_n} \end{bmatrix} \quad (2)$$

The Markov parameters are given by

$$m_0 = D$$

$$m_1 = CB$$

$$m_2 = CAB$$

\vdots

$$m_k = CA^{k-1}B$$

\vdots

$$m_{2n-1} = CA^{\frac{2n-1}{2}}B$$

(3)

which can be measured by a method developed by Liu and Suen [5].

Once the Markov parameters, m_i , $i = 0, 1, \dots, 2n-1$, are obtained, the circuit parameters R's and C's can be solved from the simultaneous equations (2) and (3).

In this simulation, it assumes no measurement error for both $Z(s)$ and m_i 's. They are exact. We want to find the numerical error generated by solving (1) and (3).

Ladders of four and six stages were chosen, transfer functions and A, B, C, D parameters were calculated using nominal values of components. Then, as a way of comparison, the significant digits of coefficients of transfer function and entries of A, B, C, D were reduced before we performed the manipulation by these two methods. The results are listed in Tables 1 and 2.

It is clear from the tables that, as significant digits decrease, the estimated values of frequency-domain method stray away from nominal values gradually, then collapse abruptly at a certain point and become unrealizable, i.e., some of the values become negative. On the contrary, the results of the time-domain method remain about the same order of accuracy as parameters of state equation.

The discrepancies may be due to the following reasons:

- 1) The frequency-domain approach deals with computations of complex numbers while the time-domain approach deals with computations of real numbers.
- 2) The given circuit is sequentially-linear for the time-domain approach [5,6]. This can be demonstrated by the 4-stage RC ladder. Solving (2) and (3), we have

$$m_0 = R_1$$
$$m_1 = \frac{1}{C_1}$$

$$m_2 = -\frac{1}{R_2 C_1^2}$$

$$m_3 = \frac{1}{R_2^2 C_1^2} \left(\frac{1}{C_1} + \frac{1}{C_2} \right)$$

Therefore, R_1 , C_1 , R_2 , C_2 can be solved sequentially by a set of linear equations,

$$R_1 = m_0$$

$$C_1 = \frac{1}{m_1}$$

$$R_2 = -\frac{1}{m_2 C_1^2}$$

$$\frac{1}{C_2} = m_3 R_2^2 C_1^2 - \frac{1}{C_1}$$

III. Conclusion

This simulation strongly suggests that time-domain approach is more data-tolerant than frequency-domain approach in the sense that no sudden breakdown occurs and component values can be estimated with reasonable accuracy when the measurement is not accurate enough or where the noise must be taken into consideration. Thus, though it is still too early to have definite conclusion, time-domain approach seems to be a more promising method in attacking fault diagnosis problem.

Simulation on 4-stage RC Ladder

	Time-Domain Method				Frequency-Domain Method			
	R_1 C_1	R_2 C_2	R_3 C_3	R_4 C_4	R_1 C_1	R_2 C_2	R_3 C_3	R_4 C_4
Nominal Values	2.2 .015	47 .47	8.2 .01	1 .022	2.2 .015	47 .47	8.2 .01	1 .022
Significant Digits	2.2 .015	47 .47	8.2 .01	1 .022	2.2 .015	47 .47	8.2 .01	1 .022
10	2.2 .015	47 .47	8.2 .01	1 .022	2.2 .015	47 .46597	1.3587 .0056867	7.7603 .030347
8	2.2 .015	47 .47	8.2 .01	1 .022	2.2 .015	47.005 .70919	-.018072 -.23768	9.1305 .030482
7	2.2 .015	47 .47	8.2 .01	1 .022				
6	2.2 .015	47 .47	8.2 .01	1 .022				
4	2.2 .014999	47.017 .46982	8.2044 .0099962	1.0003 .021997				
2	2.2 .014925	47.857 .46434	8.4454 .0096776	1.0569 .020555				

Table 1: In the frequency-domain approach, the calculated values of R_3 and C_3 become negative when the significant digits are reduced to 7. No such discrepancies in the time-domain approach.

Simulation on 6-Stage RC Ladder

		Time-Domain Method						Frequency-Domain Method					
		R ₁	R ₂	R ₃	R ₄	R ₅	R ₆	R ₁	R ₂	R ₃	R ₄	R ₅	R ₆
		C ₁	C ₂	C ₃	C ₄	C ₅	C ₆	C ₁	C ₂	C ₃	C ₄	C ₅	C ₆
Nominal Values	15	220	39	75	8.2	100		15	220	39	75	8.2	100
	.0022	.001	.015	.022	.0047	.01		.0022	.001	.015	.022	.0047	.01
Significant Digits	15	220	39	75	8.2	100		15	220	39	75	8.206	99.994
	.0022	.001	.015	.022	.0047	.01		.0022	.001	.015	.022	.004696	.01
10	15	220	39	75	8.2	100		15	220	39	75.027	8.9232	99.25
	.0022	.001	.015	.022	.0047	.01		.0022	.001	.015	.022436	.0042666	.0099976
8	15	220	39	75	8.2	100		15	220	39	75	8.9232	99.25
	.0022	.001	.015	.022	.0047	.01		.0022	.001	.015	.022436	.0042666	.0099976
7	15	220	39	75	8.2	100		15	220	39.003	74.992	8.0302	100.18
	.0022	.001	.015	.022	.0047	.01		.0022	9.9994E-4	.015	.021883	.0048168	.010001
6	15	220	39	74.999	8.1999	100		15	219.98	39.023	77.659	- .67597	106.2
	.0022	.001	.015	.022	.0047001	.0099997		.0022	.0010004	.015015	- .022917	.049583	.010019
4	15	219.99	38.988	74.908	8.1865	100.16							
	.0022002	.0010001	.015011	.022036	.0047074	.0099507							
2	15	214.29	37.815	75.63	8.6555	120.64							
	.0022222	.001037	.015256	.021107	.0044222	.0073993							

Table 2: In the frequency-domain approach, the calculated values of C₄ and R₅ become negative when the significant digits reduced to 6. No such discrepancies in the time-domain approach.

References

- [1] R. Saeks, S.P. Singh and R.W. Liu, "Fault Isolation via Components Simulation", IEEE Transaction on Circuit Theory, Vol. CT-19, No. 6, pp. 634-640, November, 1972.
- [2] N. Sen and R. Saeks, "Fault Diagnosis for Linear Systems Via Multifrequency Measurements," IEEE Trans. on Circuits and Systems, Vol. CAS-26, pp. 457-465, 1979.
- [3] T.N. Trick, W. Mayeda and A.A. Sakla, "Calculation of Parameter Value from Node Voltage Measurements," IEEE Trans. on Circuits and Systems, Vol. CAS-26, pp. 466-474.
- [4] R. Liu and L.C. Suen, "Minimal Dimension Realization and Identifiability of Input/Output Sequence," IEEE Trans. on Automatic Control, April 1977.
- [5] R. Liu and V. Visvanathan, "Sequentially Linear Fault Diagnosis: Part I-Theory," IEEE Trans. on Circuits and Systems, Vol. CAS-26, pp. 490-496, 1979.
- [6] V. Visvanathan, "Sequentially Linear Fault Diagnosis: Part II-The Design of Diagnosable Systems," IEEE Trans. on Circuits and Systems, Vol. CAS-26, pp. 558-564, 1979.